

(25%) 1. Give definitions for each of the following standard Haskell functions; for each function, also include a *comment* (in the format used in this module) to clearly and concisely describe its purpose:

a)	take	<p>Q1A -- take n xs Take n items from the list xs ^{negative} ✓</p> <p>take :: Int -> [a] -> [a] ✓</p> <p>take n [] = []</p> <p>take n (x:xs) n > 0 = x + take (n-1)(xs)</p> <p> otherwise = [] ✓</p> <p>Used when trying to get the first n items from any list</p> <p>-- take n xs, take n items from the list xs</p> <p>-- Used when we want to try and get rid of the first n items</p> <p>take n[] = []</p> <p>take n(x:xs) n>0 = x take (n-1)(xs) otherwise = []</p>	<p>24</p> <p>5</p>
b)	drop	<p>Q1B -- drop n xs Drop the first n items from the list xs</p> <p>drop :: Int -> [a] -> [a]</p> <p>drop n [] = []</p> <p>drop n (x:xs) n > 0 = drop (n-1)(xs)</p> <p> otherwise = (x:xs) ✓</p> <p>Used when to get rid of the first n items from any list</p> <p>-- drop n xs drop the first n items from the list xs</p> <p>-- Used when we want to get rid of the first n items from any list</p> <p>drop n[] = []</p> <p>drop n(x:xs) n>0 = drop(n-1)(xs) otherwise = (x:xs)</p>	<p>5</p>

c)	takeWhile	<p>Q1 c -- takeWhile p xs Take the first set of items from xs that match the predicate p</p> <p>takeWhile p [] = [] 5</p> <p>takeWhile p (x:xs) (p x) = x : takeWhile p (xs) otherwise = []</p> <p>Used when we want a list made up of the first so many items in a list that match the predicate p</p> <p>Type: takeWhile :: (a -> Bool) -> [a] -> [a]</p> <p>-- takeWhile p xs take the first set of items from xs that match the predicate p -- Used when we want a list made up of the first so many items in a list that match the predicate p</p> <p>takeWhile p [] = []</p> <p>takeWhile p (x:xs) (p x) = x : takeWhile p (xs) otherwise = []</p>
d)	dropWhile	<p>Q1 d -- dropWhile p xs drop the first sequence of elements in xs that all match predicate p</p> <p>dropWhile :: (a -> Bool) -> [a] -> [a]</p> <p>dropWhile p [] = []</p> <p>dropWhile p (x:xs) (p x) = dropWhile p (xs) otherwise = x : xs 5</p> <p>Used when we want to drop the first so many elements in a list which match a predicate</p> <p>-- dropWhile xs drop the first sequence of elements in xs that all match predicate p. -- Used when we want to drop the first so many elements in a list which match a predicate.</p> <p>dropWhile :: (a -> bool) -> [a] -> [a]</p> <p>dropWhile p [] = []</p> <p>dropWhile p (x:xs) (p x) = dropWhile p (xs) otherwise = x : xs</p>
e)	zipWith	<p>Q1 e -- zipWith f xs ys combine the elements of xs with the elements of ys using f until either list is empty</p> <p>zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]</p> <p>zipWith _ _ [] = [] 4</p> <p>zipWith _ [] _ = []</p> <p>zipWith f (x:xs) (y:ys) = (f x y) : zipWith f (xs) (ys)</p>

-- zipWith f x ys combine the elements of xs with the elements of ys using f until either list is empty.

zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]

zipWith _ _ [] = []

zipWith _ [] _ = []

zipWith f (x:xs) (y:ys_) = (f x y) : zipWith f (xs) (ys)

(35%) 2. A *stairs* is a finite list of two or more integers such that the difference between every pair of adjacent items is a non-zero constant. For example, each of these lists is a stairs:

[5, 8] [1, 3, 5, 7, 9] [3, 2, 1, 0, -1, -2]

whereas none of these lists is a stairs:

[] [4] [1, 3, 5, 8, 9] [1, 2, 3, 2, 1] [7, 7, 7].

Write a Haskell function `isStairs` to test if a given finite list of integers is a stairs.

Answer ???

$$\text{isStairs} :: [\text{Integer}] \rightarrow \text{Bool}$$

$$\text{isStairs } (x_1 : x_2 : x_3) \mid (x_1 - x_2) == 0 = \text{False}$$
 WHAT IF LENGTH 0 OR 1? | otherwise isDifferentBy (x1-x2) (x2:x3)

-- isDifferentBy n xs does every item in xs differ by the number n

$$\text{isDifferentBy} :: \text{Num } a \Rightarrow a \rightarrow [a]$$

$$\text{isDifferentBy } _ [] = \text{True}$$

$$\text{isDifferentBy } n (x_1 : x_2 : x_3) = (x_1 - x_2 == n) \ \&\& \ \text{isDifferentBy } n (x_2 : x_3)$$

$$\text{isDifferentBy } _ (x : []) = \text{True}$$
 or: [-]

30

isStairs :: [Integer] -> Bool

isStairs (x1:x2:x3) | (x1 - x2) == 0 = False | otherwise isDifferentBy (x1-x2)(x2:x3)

-- isDifferentBy n xs does every item in xs differ by the number n

isDifferentBy _ [] = True

isDifferentBy n(x1:x2:x3) && isDifferentBy n(x2:x3)

isDifferentBy _(x:[]) = True

(40%) 3. a) Give a Haskell definition for the function `iterate`, which takes a function $f :: a \rightarrow a$ and an item $x :: a$ as parameters, and returns the infinite list:

[x, f x, f (f x), f (f (f x)), ...].

(10%)

Answer

Q3 a $iterate :: (a \rightarrow a) \rightarrow a \rightarrow [a]$

7 $iterate\ f\ x = x : iterate\ (f\ x)\ f$

$f\ (f\ x)$

$iterate :: (a \rightarrow a) \rightarrow a \rightarrow [a]$
 $iterate\ f\ x = x : iterate\ f\ (f\ x)$

b) Give a Haskell definition for the infinite list `reps`, which has, as its n^{th} item, a list composed of n copies of the integer n , for $n = 1, 2, 3, \dots$; thus, `reps` is the list: $[[1], [2, 2], [3, 3, 3], [4, 4, 4, 4], \dots]$.
 (as preparation for part (c), consider using `iterate` to solve this problem). (15%)

Answer

Q3 b $reps :: [[Integer]]$

$reps = \underset{map}{iterate} copies [1..]$ or from 1

10 $-- copies\ n\ The\ list\ of\ n\ copies\ of\ n$

$copies :: a \rightarrow [a]$

$copies\ n = repeat\ n\ n$

$-- repeat\ x\ n\ Repeat\ item\ x\ n\ times$

$repeat :: Integer\ b \Rightarrow a \rightarrow b \rightarrow [a]$

$repeat\ x\ n\ | n > 0 = x : repeat\ x\ (n-1)$
 $| otherwise = []$

$reps :: [[Integer]]$
 $reps = map\ copies\ [1..]$

$-- copies\ n, the\ list\ of\ n\ copies\ of\ n$
 $copies :: a \rightarrow [a]$
 $copies\ n = repeat\ n\ n$

$-- repeat\ x\ n, repeat\ item\ x\ n\ times$
 $repeat :: Integer\ b \Rightarrow a \rightarrow b \rightarrow [a]$
 $repeat\ x\ n\ | n > 0 = x : repeat\ x\ (n-1) | otherwise = []$

c) *Pascal's Triangle* is an infinite triangular pattern of integers, in which each number on the boundary is 1 and each number in the interior is the sum of the two numbers diagonally above it:

```

      1
     1 1
    1 2 1
   1 3 3 1
  1 4 6 4 1
 . . . . .

```

Give a Haskell definition for the infinite list `pascal`, which has, as its n^{th} item, a list of the numbers in the n^{th} row of Pascal's Triangle, for $n = 1, 2, 3, \dots$; thus, `pascal` is the list:

`[[1], [1, 1], [1, 2, 1], [1, 3, 3, 1], ...]`. (15%)

Answer 4 Marks ???

`Pascal :: [[Integer]]`

`Pascal =`

`-- iterate over lists [[1], [1,2], [1,2,3], ...]`

applying `pascal'` to each item in that list
making it back into a new list

`-- pascal' n x` ← type? `Int -> Int -> Int ?`

Get the x^{th} Pascal item at row n

`pascal' 0 = 1`

`pascal' n x | x == n = 1`

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`|x = pascal' (n-1) (x-1) +`

`| pascal' (n-1) x`

condition
to keep
it in bound

| otherwise = 0

(didn't have
enough time to
work it out)